

Flywheel Spinup Dynamic Model

Parameters:

W_o motor free speed
 T_s motor stall torque
 J flywheel inertia
 G gearbox speed reduction
 K_f gearbox efficiency fraction
 K_s speed-dependent torque loss

Variables:

T_f torque at flywheel
 T_m motor torque
 W_m motor speed
 W_f flywheel speed

Equations:

$W_m = G \cdot W_f$
 $T_m = T_s \cdot (1 - W_m / W_o)$
 $T_f = K_f \cdot G \cdot T_m - K_s \cdot W_m$
 $d(W_f) / dt = T_f / J$

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(%i1) Wm: G*Wf;
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```
(%o1) Wf G
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(%i2) Tm: Ts*(1-Wm/Wo);
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(%o2) Ts \left( 1 - \frac{Wf G}{Wo} \right)
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(%i3) Tf: Kf*G*Tm - Ks*Wm;
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(%o3) Kf Ts G \left( 1 - \frac{Wf G}{Wo} \right) - Ks Wf G
```

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(%i4) dWfdt = Tf/J;
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```
(%o4) dWfdt = \frac{Kf Ts G \left( 1 - \frac{Wf G}{Wo} \right) - Ks Wf G}{J}
```