## 3 parameter friction/loss model

- k3 = torque-dependent drivetrain friction torque losses (drivetrain efficiency fraction)
- k2 = speed-related rolling resistance force losses (carpet compression)
- k1 = misc constant force losses

## Heun's integration

- 2nd order integration, superior speed and accuracy compared to Euler
- Heun's can use 0.01 time steps and be as accurate as Euler with 0.001 steps
- Heun's integration explained: http://calculuslab.deltacollege.edu/ODE/7-C-2/7-C-2-h.html

### Full C source code

- the compiled executable writes to standard output
- redirect the output to "filename.CSV", which can be opened directly in Excel for graphing
- easy to edit the constants in the C code to reflect your drivetrain design
- easy to change the output format to target other graphing programs such as gnuplot<sup>1</sup>
- easy to write a "glue" script (BAT file) to automate the process of editing, compiling, running, and graphing

# Engineering units

- SI units used internally for simplicity of computation
- English-to-SI conversions provided in source code so user can enter constants in English units
- SI-to-English conversions provided in source code for outputs

### Model assumptions

- spec motor voltage is applied at t=0 (see footnote<sup>2</sup>)
- all weight-bearing wheels are driven
- equal weight distribution on all wheels
- all wheels have the same "slipping" state
- transition from "slipping" to "not slipping" occurs instantaneously<sup>3</sup>

<sup>&</sup>lt;sup>1</sup> highly recommended: www.gnuplot.info

 $<sup>^{2}</sup>$  voltages other than 12 can be accomodated by adjusting the values of Ts and Mfree accordingly  $^{3}$  with no energy transfer due to speed mismatch between vehicle and wheels

# For the example I used:

- 4 CIM motors (n=4; Ts=343.4 in-oz; Mfree=5310 RPM); - k1=10 lbf; - k2=1 lbf/(ft/s); - k3=0.9 - G=12.75 - r=3 inches - M=150 lbs - uk=0.7 - us=1.0 - dt=0.001 (1 ms time step for numerical integration)

For this example I picked k1, k2, and k3 out of the ether. For an accurate model you will want to determine these experimentally for your drivetrain. It would be enlightening to have a discussion about accurate and simple tests that could be used to determine these constants.